

Limitations of Deep Learning

Oliver Richter

AI pioneer Geoff Hinton: “Deep learning is going to be able to do everything”

Thirty years ago, Hinton’s belief in neural networks was contrarian. Now it’s hard to find anyone who disagrees, he says.

by **Karen Hao**

November 3, 2020

```
graph TD; A([End-to-End Training]) --- B([More Parameters]); A --- C([Deeper Models]);
```

End-to-End
Training

More
Parameters

Deeper
Models

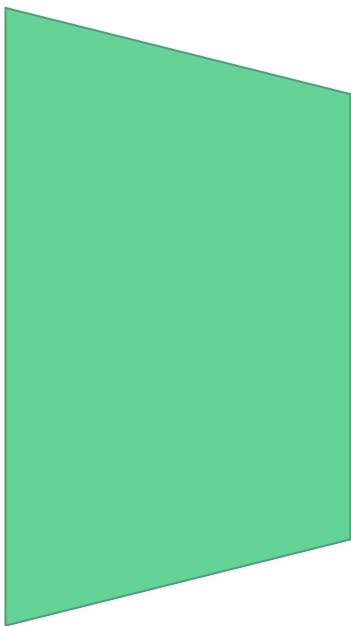
Why should you do it?

End-to-End
Training



Why should you do it?

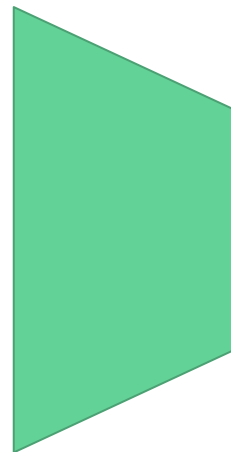
End-to-End
Training



“Cat”

“Dog”

“House”



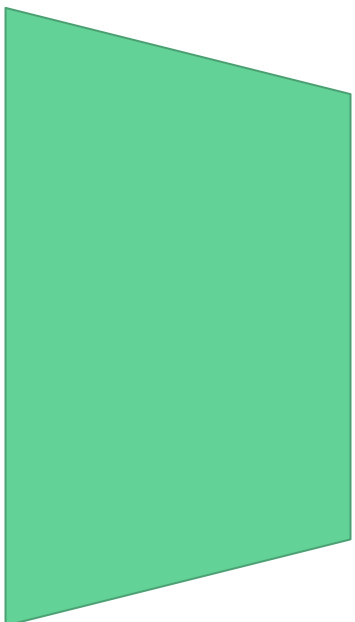
“Animal”

“No animal”

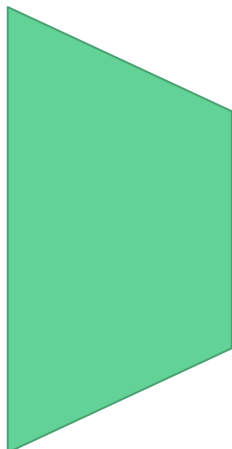


What happened?

End-to-End
Training



“Cat”
“Dog”
“**House**”



“Animal”
“**No animal**”

What happened?

End-to-End
Training



Impossible?

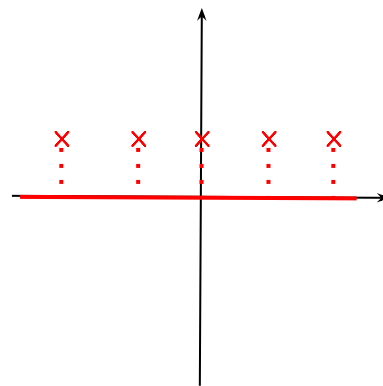
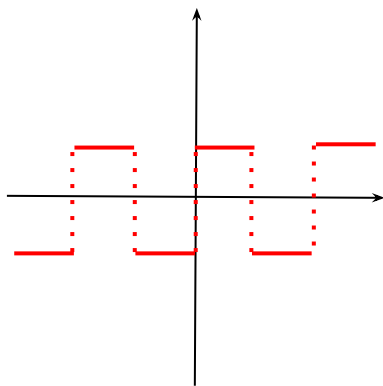
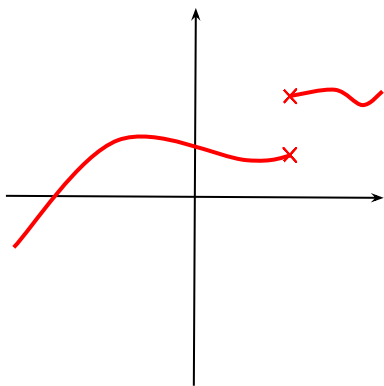
“Animal”

“No animal”

What's the catch?

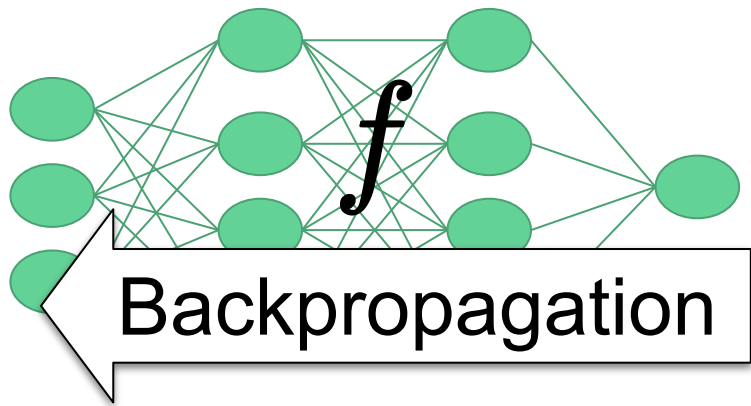
End-to-End
Training

Neural networks cannot learn to represent discontinuous functions.



Why?

End-to-End
Training

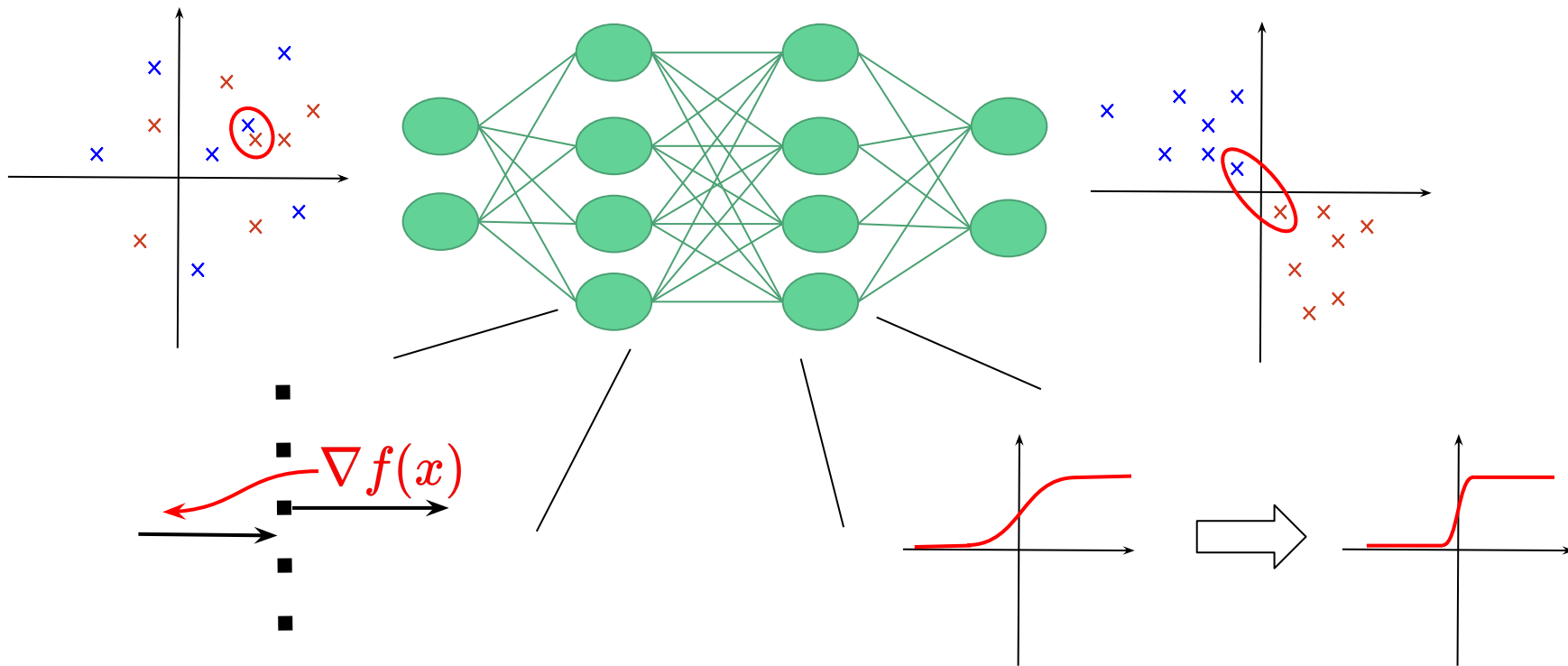


f continuous

$$\begin{array}{c} \text{L-shaped arrow pointing right} \\ \exists \nabla_x f(x) \forall x \text{ L-shaped arrow pointing up} \end{array}$$

Is it that bad?

End-to-End Training



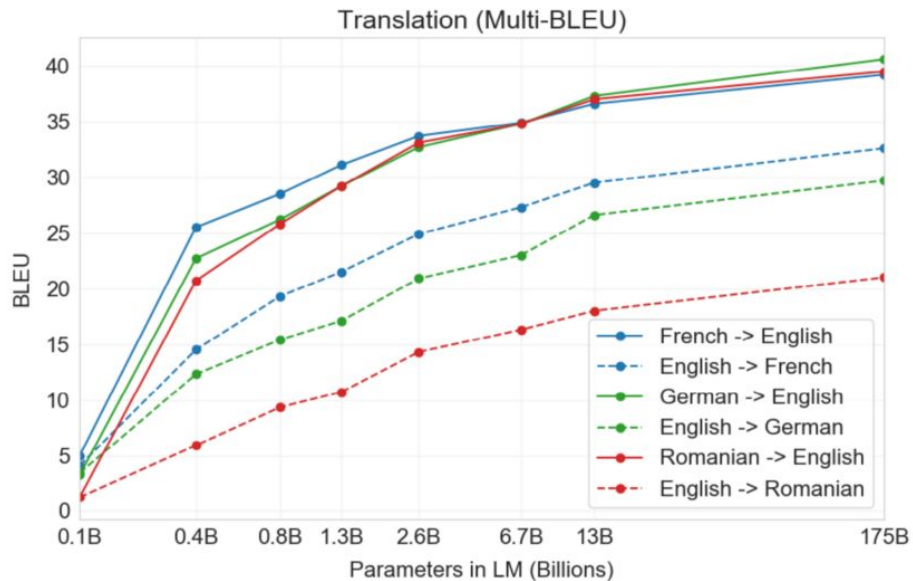
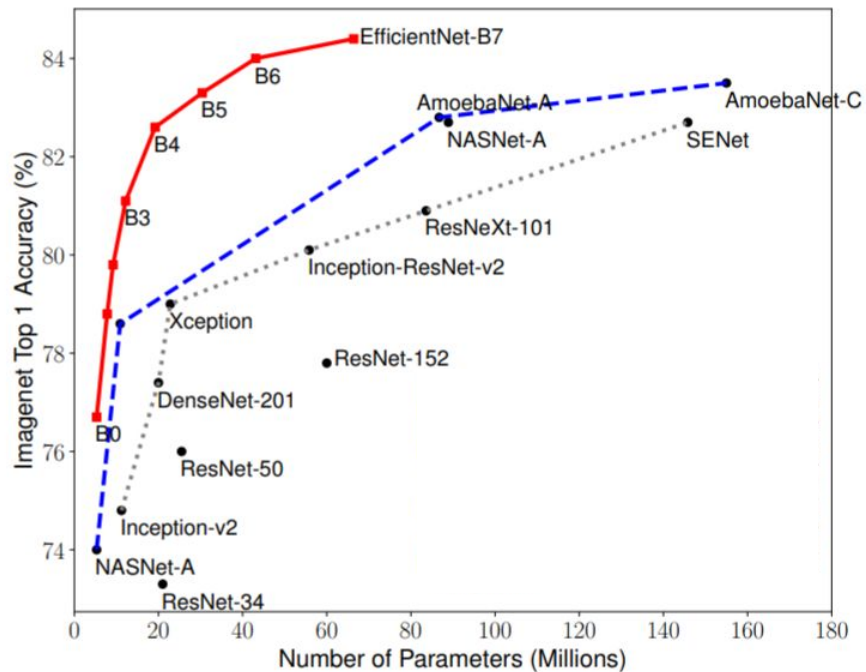
End-to-End
Training

More
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Deeper
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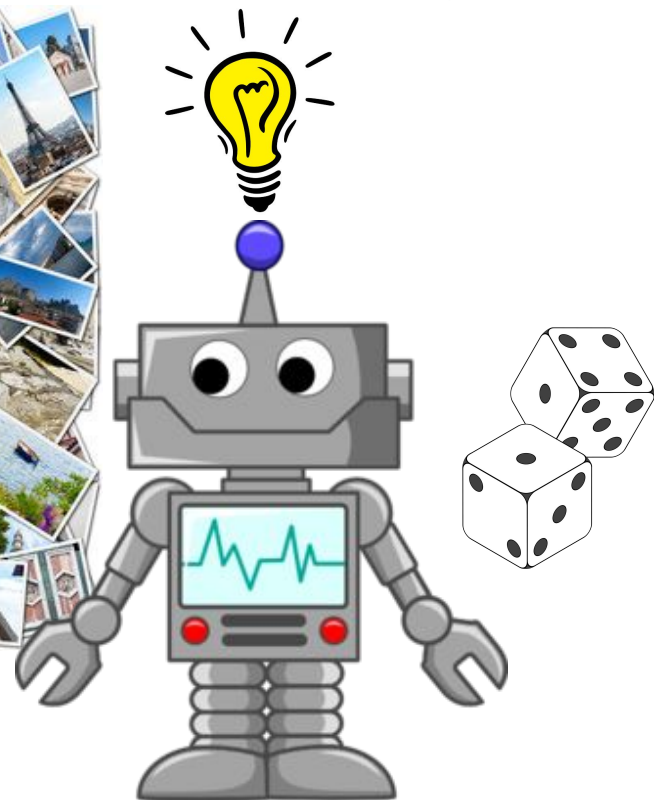
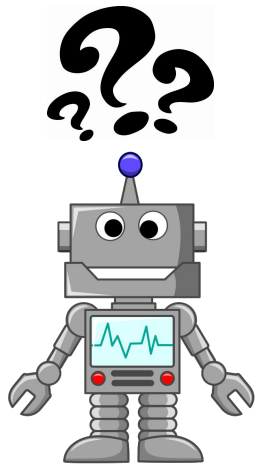
Why should you do it?

More Parameters

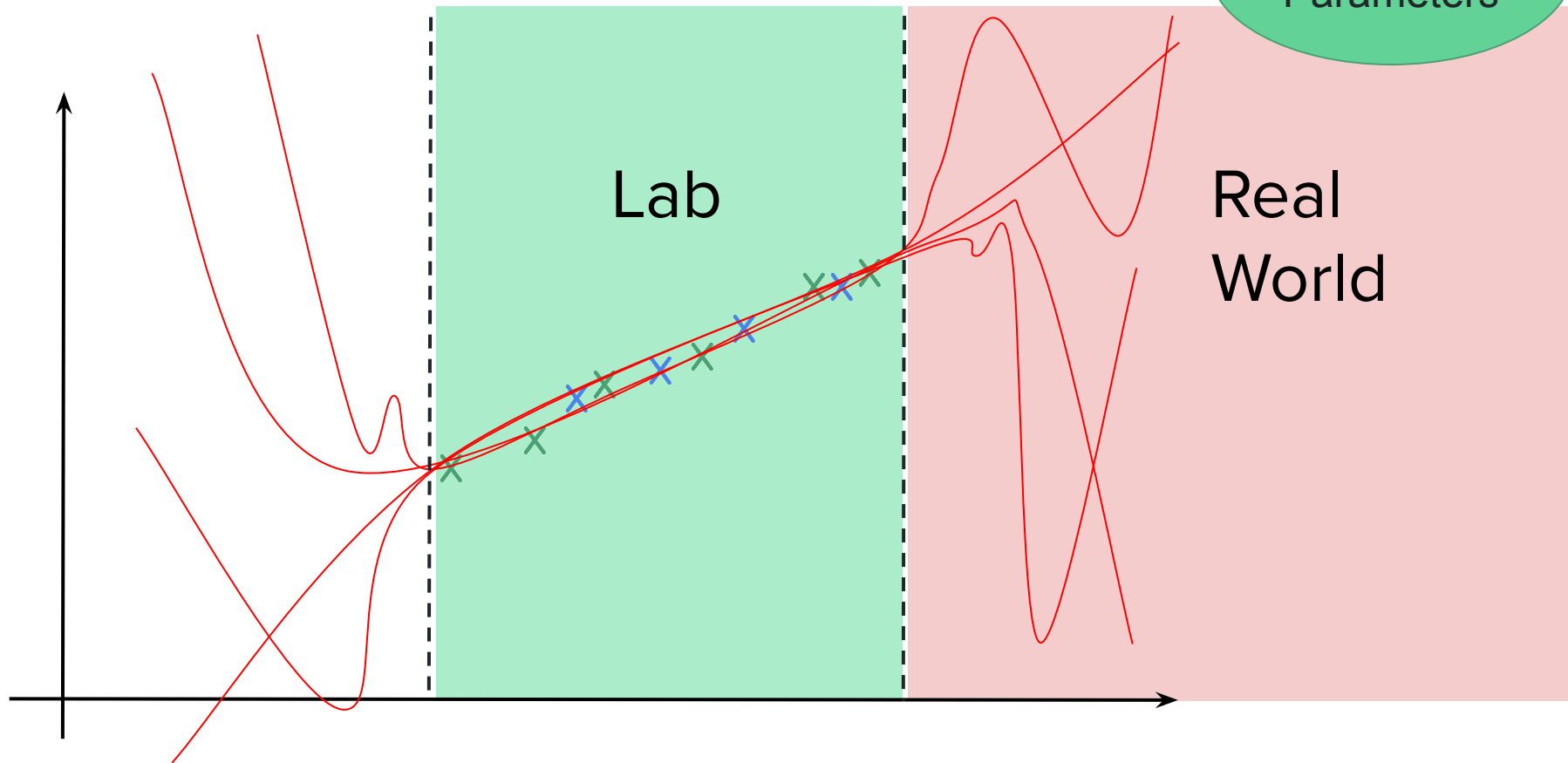


Why should you do it?

More
Parameters



What's the catch?



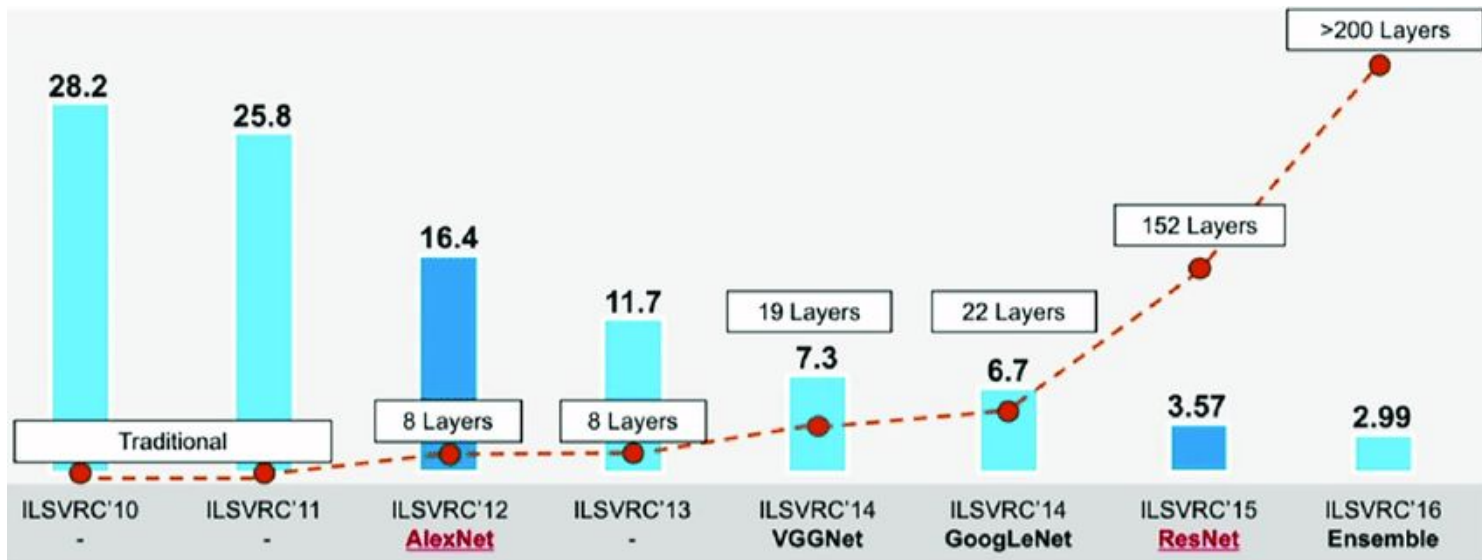
End-to-End
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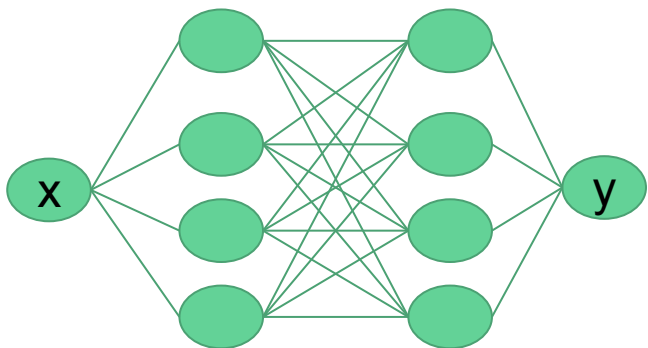
Why should you do it?

Deeper Models

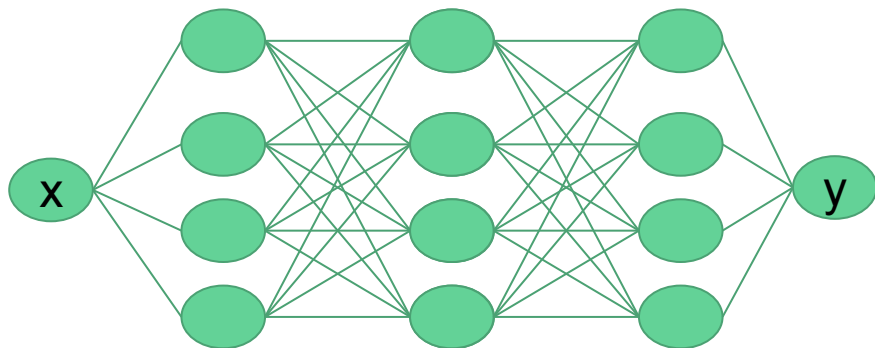


Why should you do it?

Deeper Models



n^2 paths



n^3 paths

$$\#params \in \mathcal{O}(L \cdot n^2)$$

$$\#paths \in \mathcal{O}(n^L)$$

What's the catch?

$$\|A\|_{op} = c \rightarrow \|Av\| \leq c\|v\|$$

$$c_l = \|W_l^T\|_{op} \quad c_\sigma \leq 1$$

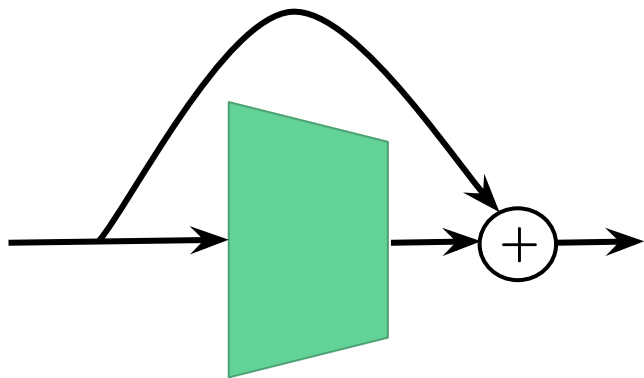
$$\|\nabla_x f(x)\| \leq \|\nabla_y f(x)\| \cdot \prod_{l=1}^L c_l \cdot c_\sigma$$

$c_l < 1 \rightarrow$ vanishing gradients

Solutions?

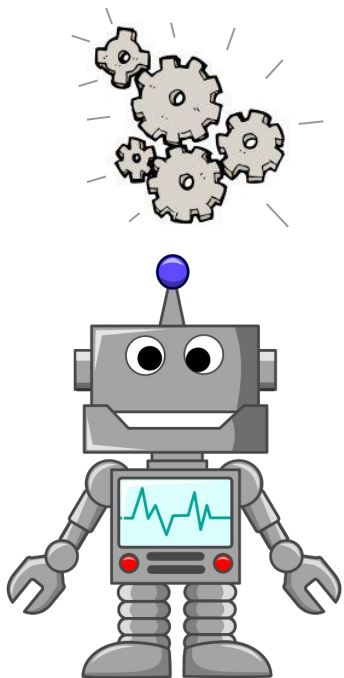
Deeper
Models

- Initialization
- Constraint Optimization
- Residual Connections



Other Problems with Depth?

Deeper
Models

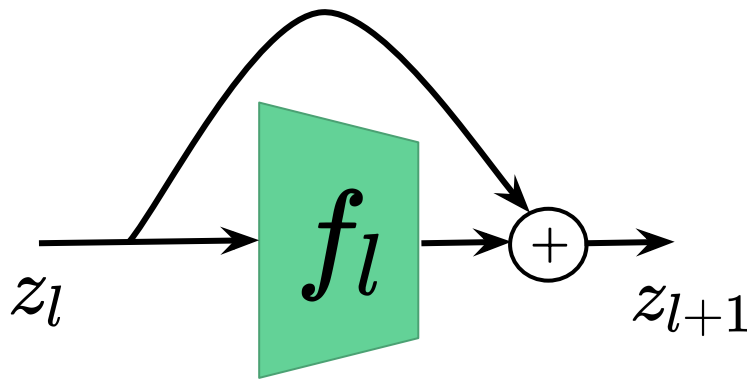


$$\mathcal{O}(L)$$



Implicit Layers

Deeper
Models



$$z_{l+1} = z_l + f_l(z_l)$$

$$z_L = z_0 + \sum_{l=0}^L f_l(z_l)$$

Implicit Layers

Deeper
Models

$$z(L) = z(0) + \sum_{l=0}^L f(z(l), l)$$

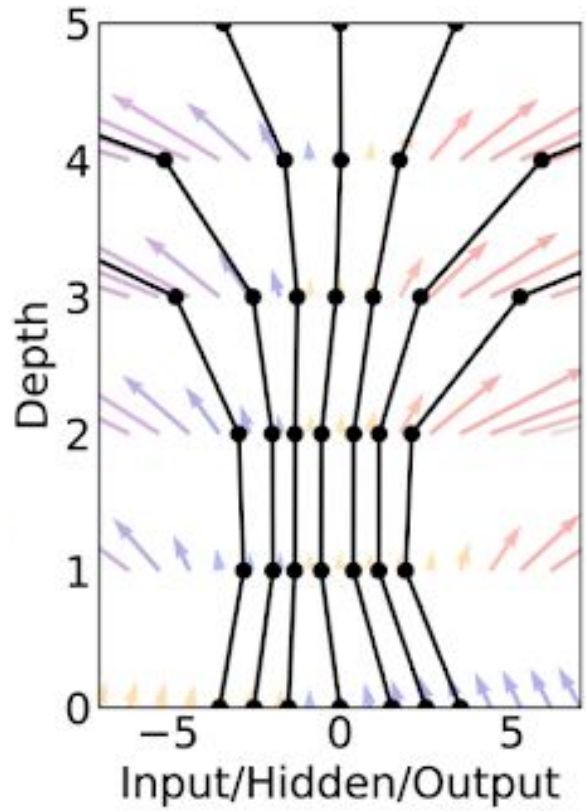
$$z(L) = z(0) + \int_0^L f(z(l), l) dl$$

$$\frac{dz}{dl} = f(z(l), l)$$

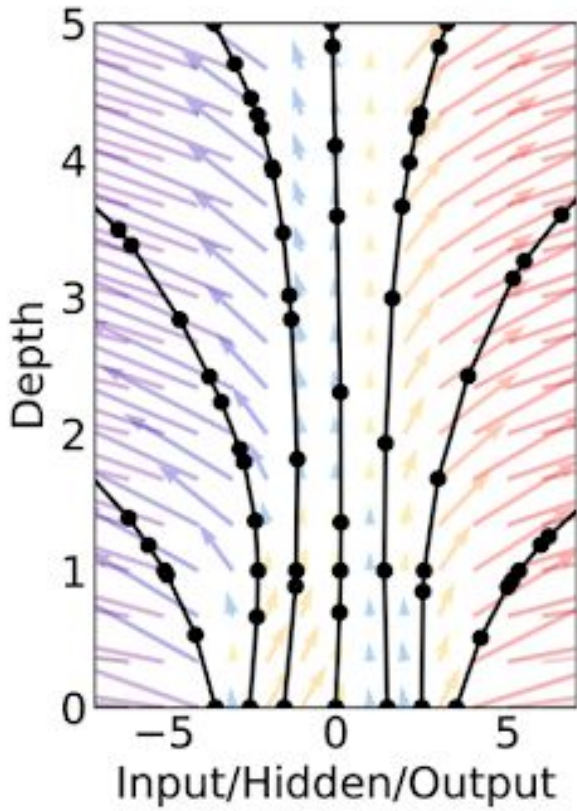
Given f , z_0 use ODE solver to find z_L

Deeper Models

Residual Network



ODE Network



How to train?

Deeper
Models

$$\frac{\delta \mathcal{L}}{\delta \theta} = \sum_l \frac{\delta \mathcal{L}}{\delta z_{l+1}} \frac{\delta f(z_l, \theta)}{\delta \theta}$$

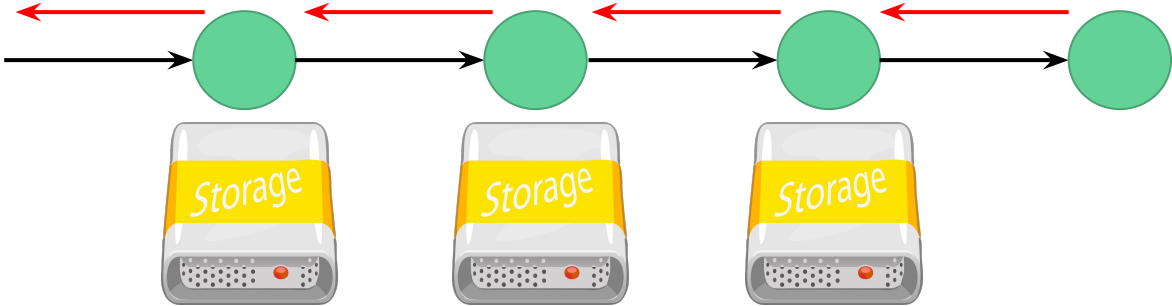
$$\frac{\delta \mathcal{L}}{\delta \theta} = \int_L^0 \frac{\delta \mathcal{L}}{\delta z(l)} \frac{\delta f(z(l), \theta)}{\delta \theta} dl$$

→ Use ODE solver

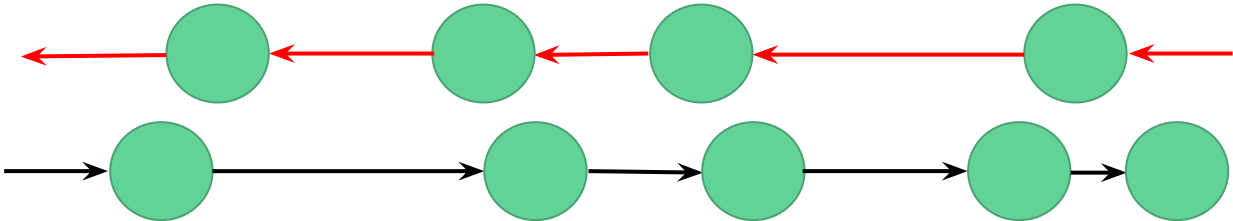
$\mathcal{O}(1)$



Deeper Models



$\mathcal{O}(L)$

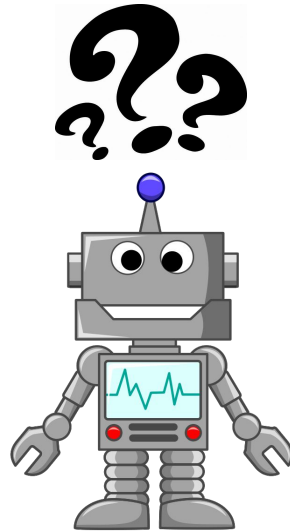


$\mathcal{O}(1)$



End-to-End
Training

More
Parameters



Deeper
Models