

# Localization in Sensor Networks

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# Localization

- Active Localization
  - System sends signals to localize target
  - eg. Radar(non-cooperative), GPS(cooperative)
- Passive Localization
  - System deduces location from observation of signals that are *already present*
  - eg. Signals normally emitted by the target (eg. birdcalls)

# Motivation

- Many applications of WSN require the knowledge of where the individual nodes are located
- Motivating examples: Countersniper systems, Animal Tracking and Logistics
- We now look at an example of countersniper systems

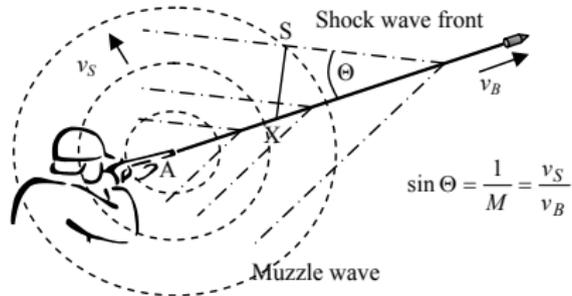
## Problem and Challenges

- To locate snipers in an urban environment
- Challenges of an urban terrain
  - Multipath effects
  - Poor coverage due to shading effect of buildings
- Limitations of existing systems
  - Require direct line of sight
  - Rely on muzzle flash that can be suppressed
  - Centralized, thus not robust to sensor failure
- Cost effectiveness

# Solution

- Use an ad-hoc wireless sensor network-based system
- Utilize many cheap sensors for
  - good coverage of direct signal
  - tolerance to failures
- Detect via acoustic signals like muzzle blasts and shockwaves

# Acoustic Signals



**Figure 1:** Acoustic events generated by a shot. The muzzle blast produces a spherical wave front, traveling at the speed of sound ( $v_S$ ) from the muzzle ( $A$ ) to the sensor ( $S$ ). The shock wave is generated in every point of the trajectory of the supersonic projectile producing a cone-shaped wave front, assuming the speed of the projectile is constant  $v_B$ . The shockwave reaching sensor  $S$  was generated in point  $X$ . The angle of the shockwave cone is determined by the Mach number ( $M$ ) of the projectile.

# PinPtr

- Ad-hoc wireless network of inexpensive sensors
- Sensors can
  - detect muzzle blasts and acoustic shockwaves
  - measure their time of arrival (TOA)
- Message routing service delivers TOA to a base station
- User Interface through base stations or PDAs
- System field tested at the US Army McKenna MOUT (Military Operations in Urban Terrain) facility at Fort Nenning, GA

# System Architecture

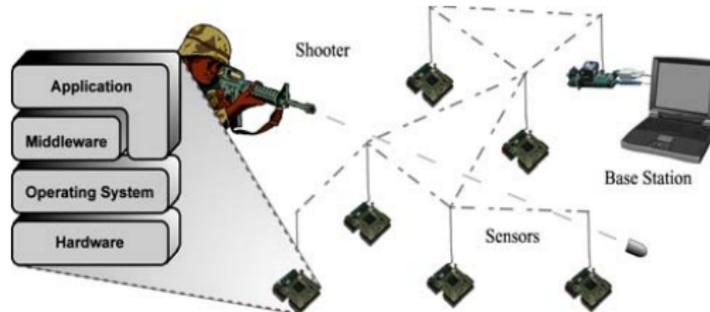


Figure 2: System Architecture

# Middleware Services

- Time Synchronization
  - Flooding Time Synchronization Protocol
  - All nodes synchronized with a root node
- Message Routing
  - Gradient-based best effort converge-cast protocol
  - All data routed to a root node
- Sensor Localization
  - Estimate the sensor position using shots
  - Current implementation places sensors by hand

# Sensor Fusion

## *Consistency Function*

- $C_\tau(x, y, z, t) = \text{count}(|t_i(x, y, z, t) - t_i| \leq \tau)$

## *Search Algorithm*

- General Bisection method
- Maximum  $10^5$  steps required

# Setup

- 56 nodes
- 20 known shooter positions
- 171 shots



Figure 3: PinPtr: Field Setup

# Shooter Localization Errors

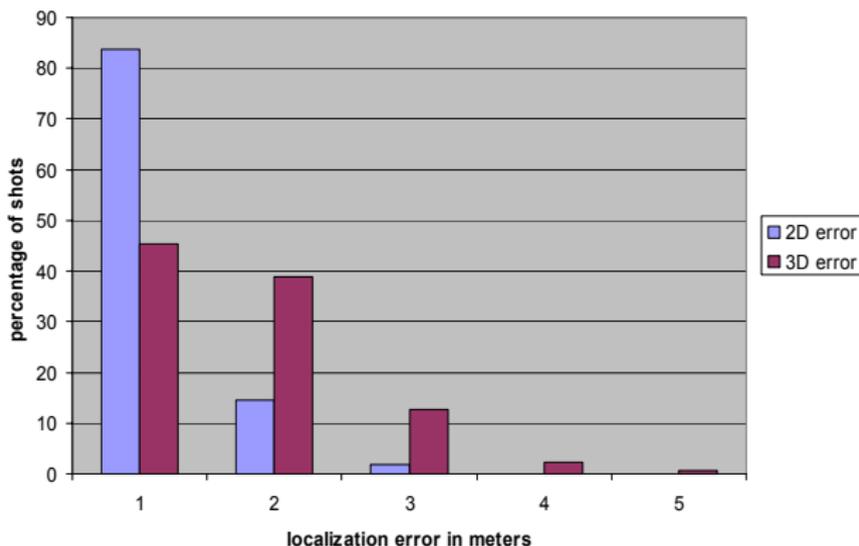


Figure 4: Localization Errors in 2D and 3D

# Error Sources

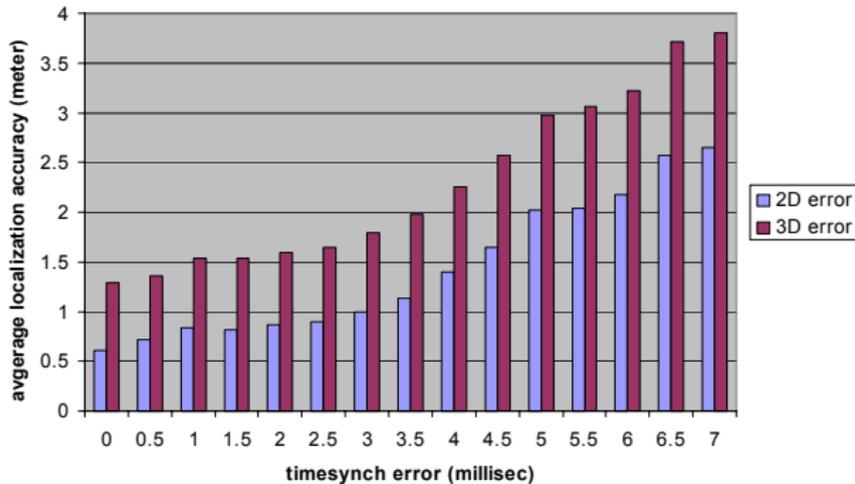


Figure 5: Localization accuracy vs. time synch error

# Sensor Density

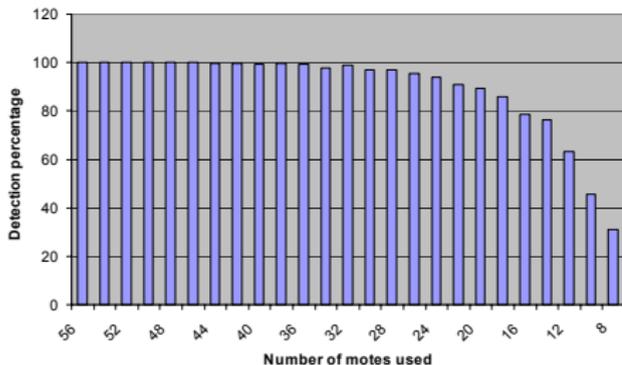


Figure 6: Detection rate vs. number of sensors used

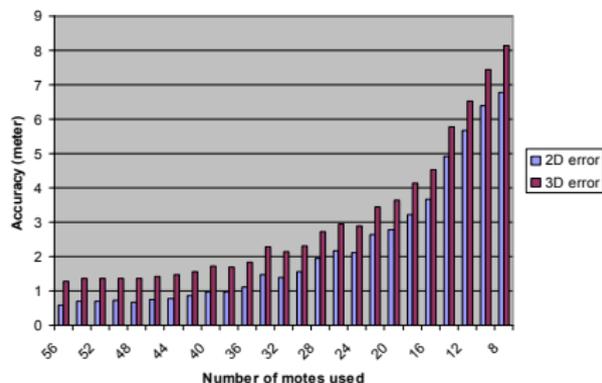


Figure 7: Localization accuracy vs. number of sensor used

# Sensor Fusion Accuracy

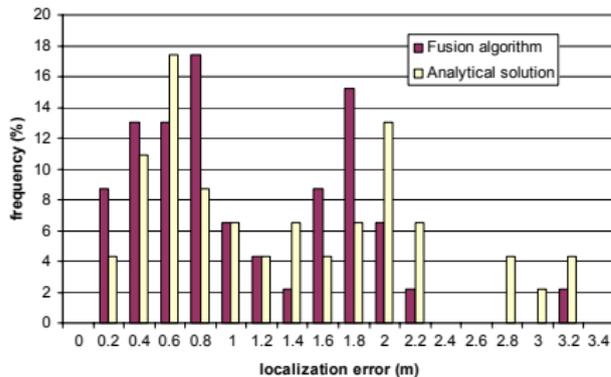


Figure 8: Error comparison with filtered readings

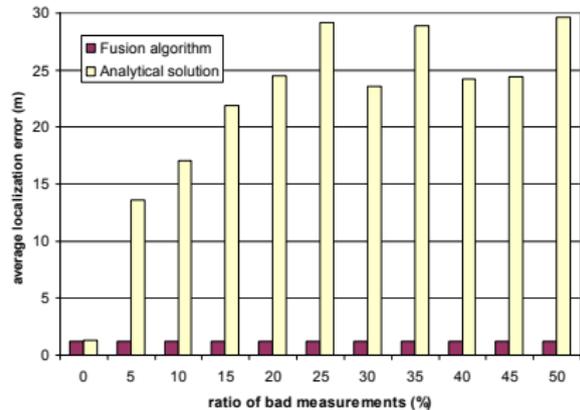


Figure 9: Error comparison with unfiltered readings

## Remarks

- Deployment of sensors in an urban environment is not trivial
- No power management
- Can not detect multiple shots
- Silencers?

# Radio Interferometry

- Pair of nodes emitting radio waves simultaneously at slightly different frequencies
- Carrier frequency of the composite signal is between the two frequencies
- Neighbouring nodes can measure the energy of the envelope signal as the signal strength

# Model

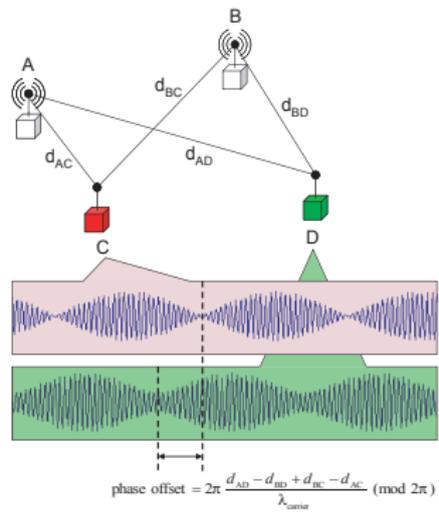


Figure 10: Radio Interferometric Ranging Technique

# Filtered RSSI Signal

Theorem 1: *Let  $f_2 < f_1$  be two close carrier frequencies with  $\delta = (f_1 - f_2)/2$ ,  $\delta \ll f_2$ , and  $2\delta < f_{cut}$ . Furthermore, assume that a node receives the radio signal*

$$s(t) = a_1 \cos(2\pi f_1 t + \varphi_1) + a_2 \cos(2\pi f_2 t + \varphi_2) + n(t),$$

*where  $n(t)$  is the Gaussian noise. Then the filtered RSSI signal  $r(t)$  is periodic with fundamental frequency  $f_1 - f_2$  and absolute phase offset  $\varphi_1 - \varphi_2$ .*

## Relative Phase Offset

Theorem 2: *Assume that the two nodes A and B transmit pure sine waves at two close frequencies  $f_A > f_B$  such that  $f_A - f_B < f_{cut}$ , and two other nodes C and D measure the filtered RSSI signal. Then the relative phase offset of  $r_C(t)$  and  $r_D(t)$  is*

$$2\pi \left( \frac{d_{AD} - d_{AC}}{c/f_A} + \frac{d_{BC} - d_{BD}}{c/f_B} \right) \pmod{2\pi}$$

## Relative Phase Offset

Theorem 3: Assume that the two nodes  $A$  and  $B$  transmit pure sine waves at two close frequencies  $f_A > f_B$ , and two other nodes  $C$  and  $D$  measure the filtered RSSI signal. If  $f_A - f_B < 2\text{kHz}$ , and  $d_{AC}, d_{AD}, d_{BC}, d_{BD} \leq 1\text{km}$ , then the relative phase offset of  $r_C(t)$  and  $r_D(t)$  is

$$2\pi \left( \frac{d_{AD} - d_{BD} + d_{BC} - d_{AC}}{c/f} \right) \pmod{2\pi}$$

where  $f = (f_A + f_B)/2$ .

# Scheduling

- At most  $n(n - 3)/2$  choices for the independent interference measurements
- In the current implementation, the base station selects all possible pairs of transmitters while all other nodes within their range act as receivers

# Tuning

- $f_1(i) = f_1 + i.325Hz, i = -15, -14, \dots, 15$
- $f_2$  constant
- Receiver analyzes  $|f_1(i) - f_2|$  which is the interference frequency
- Determine  $i$  for which the interference frequency is 0

# Time Synchronization

- Nodes need to synchronize and measure absolute phase offsets relative to a common time instant for calculating the relative phase offset
- The master broadcasts a radio message identifying the other sensor node, type of measurement, transmit power and the time to start the measurement.

# Frequency and Phase Estimation

- Peak detection performed on line in the ADC
- Post processing works exclusively on the obtained peak indexes
- Phase of the RSSI signal is estimated by the average phase of the filtered peaks

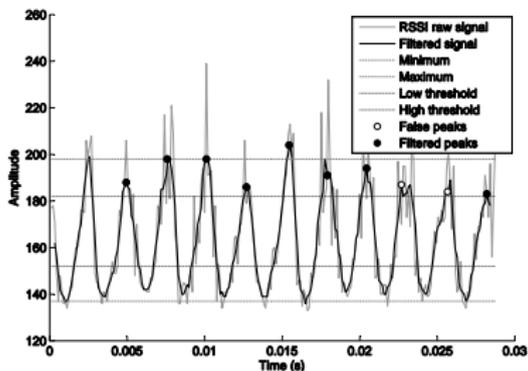


Figure 11: Peak detection and filtering

# Localization

- Generate an initial population of `populationSize` random solutions
- Select *subpopulationSize* solutions randomly from the population
- Evaluate each solution in the selected subset using the error function
- Sort the subset according to error
- Remove the worst 20% of the individuals in the sub-set, then generate new individuals by selecting random parents from the best 20% and applying genetic operators on the parents
- Go to step (2)

## Error Sources

- Carrier frequency inaccuracy
- Carrier frequency drift and phase noise
- Multipath effects
- Time synchronization error

## Effective Range

- Interferometric Radio Range ( $r$ ) is twice the range of digital communication
- $-2r \leq d_{ABCD} \leq 2r$

# Range Accuracy

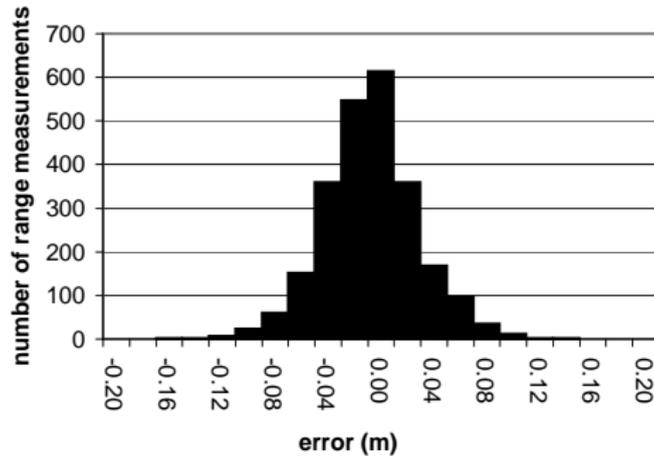


Figure 12: Central portion of the error distribution of the filtered ranges

# Localization Accuracy

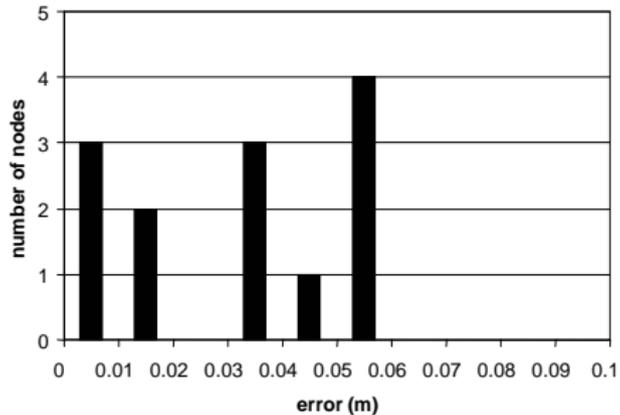


Figure 13: Error distribution of localization

# Latency

- In a 16 node network, there are approx. 32000 measurements carried out
- This entire process takes about 80 minutes.
- If we use one-fifth of the transmitter pairs, we reduce the time to 20 minutes.
- For small scale networks, the entire process can be completed in under 5 minutes.

## Remarks

- High accuracy and long range
- Supports 3D localization
- Does not require extra hardware or calibration
- High Latency
- Applications?

# Questions

Questions?