

Eidgenössische Technische Hochschule Zürich Swiss Federal Institute of Technology Zurich Distributed Computing

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## Principles of Distributed Computing Exercise 9: Sample Solution

## 1 Shared Sum

In the following, let X (initialized to 0) always denote the shared register used to hold the sum  $x = \sum_{i=1}^{n} x_i$ , and assume that all  $x_i$  (and thus also x) are initially 0. Denote by  $\Delta x_i$  the amount by which  $x_i$  is changed by process  $p_i$  at some time, i.e., if  $x_i := x_i'$  is assigned by  $p_i$ , then  $\Delta x_i = x_i' - x_i$ .

- a) To update x,  $p_i$  calls fetch-and-add $(X, \Delta x_i)$ . Therefore, X changes exactly the same as  $x_i$  and holds the correct value. Since no process has to wait or retry, we have neither lockouts nor deadlocks. A simple read on X (or fetch-and-add(X, 0)) gets the current value of x.
- **b)** An update is done by the following code:
- 1: x := X
- 2: while not compare-and-swap $(X, x, x + \Delta x_i)$  do
- x := X
- 4: end while

The loop is left after X changed by  $\Delta x_i$  exactly once, thus the code is correct. Again, x can be obtained by a simple read. Since the compare-and-swap may only fail if another process  $p_j$  changed the value of X between  $p_i$  reading it and calling compare-and-swap, there is no deadlock. However, other updates may delay a change by some  $p_i$  indefinitely, hence lockouts are possible.

c) A write is implemented by

- 1: x := load-link(X)
- 2: while not store-conditional  $(X, x + \Delta x_i)$  do
- 3: x := load-link(X)
- 4: end while

and is correct for the same reasons as in **b**). Reads are again simple. However, the solution differs from **b**) in that we may have deadlocks, since e.g. two processes can fight endlessly for getting the register linked to them for sufficiently long to write a value (At least for the case where a load-link can destroy the link to the register of another processor; i.e. weak LL/SC).

d) It can be done. We use a special encoding on X. Either it stores a regular value and  $\bot$  (i.e.,  $(x,\bot)$ ) or the value and an additional identifier identifier id(i) of a process  $p_i$ . A node will effectively acquire a lock on X by writing its ID to X and only afterwards write its update to X.

```
1: while true do
2: (x,id) := X \text{ // simple read}
3: (x,id) := \text{compare-and-swap}(X,(x,\perp),(x,id(i))) \text{ // try to lock } X \text{ with own ID}
4: if id = id(i) then
5: X := (x + \Delta x_i, \perp) \text{ // regular write, but compare-and-swap would also do}
6: break while loop
7: end if
8: end while
```

Because writing by compare-and-swap works only if the second argument equals the value of the register, once a process "locks" X with its identifier, no other process may do so until the same process performs the write enclosed in the if-condition. Thus, this write happens exactly if the compare-and-swap was successful. The only reason to check the identifier by an if-statement rather than using compare-and-swap again is that we need to ensure that the process leaves the loop after changing X by  $\Delta x_i$ . On the other hand, the while loop can only be left after a successful write, thus X is updated correctly. Reads are again plain reads.

As before, the solution is free of deadlocks: At least one process can write, because after each write the ID part of X contains  $\bot$ , i.e., one process will succeed in "locking" X. As in **b**) and **c**), the solution is prone to lockouts.